A Survey on Evolutionary Machine Learning

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ABSTRACT
Artificial intelligence emphasises the creation of intelligent machines/systems that function like humans, and has been applied to many real-world applications. Machine learning is a branch of AI based on the idea that systems can learn from data, identify hidden patterns, and make decisions with little/minimal human intervention. Evolutionary computation is an umbrella of population-based intelligent/learning algorithms inspired by nature, where New Zealand has a good international reputation. This paper provides a review on evolutionary machine learning, i.e., evolutionary computation techniques for major machine learning tasks such as classification, regression and clustering, and emerging topics including combinatorial optimisation, computer vision, deep learning, transfer learning, and ensemble learning. The paper also provides a brief review of evolutionary learning applications, such as supply chain and manufacturing for milk/dairy, wine and seafood industries, which are important to New Zealand. Finally, the paper presents emergent topics and current issues in evolutionary machine learning.

KEYWORDS
Artificial intelligence, machine learning, evolutionary computation, classification, regression, clustering, combinatorial optimisation, deep learning, transfer learning, ensemble learning.

1. Introduction

Artificial intelligence (AI) is a broad umbrella covering a wide range of techniques for building systems that can simulate human intelligence including thinking, behaviours, perception in computers. Although AI was first coined in the 1950s, its applications have flourished in just the last several decades with its core sub-area of machine learning (ML), where computers exhibit the ability to automatically learn and improve without being explicitly programmed.

ML has been applied to many applications in different domains, such as manufacturing industry, finance, and biomedical problems. Its main tasks include classification, regression, and clustering. The first two tasks are supervised learning in which a model is learnt from a set of labelled data, while the last is unsupervised learning that does not have labelled data. While classification is a task where examples/instances are classified into one of the predefined categories, regression predicts numeric outputs for
instances. However, both aims to build a model that can correctly predict the output of an unseen instance by observing a set of training labelled instances. On the other hand, clustering algorithms aim to learn a model that can group instances into separate clusters based on the intrinsic characteristics of the unlabelled data. Furthermore, solving scheduling and combinatorial optimisation problems such as determining optimal/good delivering plan and flight schedule, analysing patterns and recognising objects in computer vision also forms important research areas in ML.

Although these ML tasks have been studied for decades, challenges still arise when more large-scale datasets are collected thanks to the advanced technologies and the rapidly growing user market. Firstly, the number of features has increased over time in different domains such as images, gene expression, text and web mining (Zhang et al. 2016). This means that the search space of recent ML tasks is increasingly larger. This space could be infinite in some domains such as materials design and drug discovery (Le and Winkler 2016). Secondly, more and more complex applications are solved with or without domain expertise. Therefore, a powerful search technique is needed to find better solutions. Evolutionary computation (EC) is a sub-field of AI that comprises a family of nature-inspired algorithms. These are population-based algorithms which maintain a population of candidate solutions (or individuals) and evolve towards good/optimal solutions. By evolving multiple solutions simultaneously, EC techniques are well-known for their good global search ability.

EC techniques can be broadly divided into two main categories: evolutionary algorithms and swarm intelligence (Bäck et al. 1997). Evolutionary algorithms refer to those that apply the Darwinian natural selection principle to search for optimal solutions. Genetic algorithms (GAs) and genetic programming (GP) are two widely-used algorithms in this category. Both methods use genetic operators such as crossover and mutation to evolve new individuals. While GAs use a fixed-length bit string representation, GP can work with more flexible structures such as trees and graphs with variable sizes. On the other hand, swarm intelligence techniques are inspired by the social behaviours of animals. Typical techniques of this branch are particle swarm optimisation (PSO) and ant colony optimisation (ACO), which mimic birds and ants, respectively. While PSO works based on the information about the best found solutions shared among particles to guide the search towards more fruitful areas, ACO works by simulating the special communication system using pheromone between ants about favourable paths to food. There are also other popular EC algorithms such as differential evolution (DE), learning classifier systems (LCS), artificial immune systems (AIS), artificial bee colony (ABC) algorithms, etc.

With the ability to evolve multiple solutions simultaneously, EC techniques have shown promise in solving multi-objective problems, where optimal solutions need to be considered in the presence of two or more conflicting objectives, e.g. minimising both cost and travel time in flight booking. Because it is unlikely to have an optimal solution that satisfies both conflicting objectives, a multi-objective method returns a set of nondominated (Pareto optimal) solutions which cannot be improved in one objective without another objective suffering. Evolutionary multi-objective optimisation (EMO) becomes one of the hottest topics with dramatic increase publications in the last ten years.

EC techniques recently gain more attention in the deep learning community. Deep learning is a class of ML algorithms that use multiple layers of nonlinear processing units to solve a problem (LeCun et al. 2015). Deep learning has been successfully applied in different domains. However, designing deep learning systems still requires a significant amount of time and domain expertise. EC techniques have recently shown
promise in automating this task, which enables the creation of more advanced applications to human being.

Although a number of surveys have been done on the use of EC for machine learning tasks (EML), they either focus on a particular task such as feature selection (Xue et al. 2016), or classification using GP (Espejo et al. 2010), on a particular EC technique (Neri and Tirronen 2010), or technical orientation such as EC and ML (Zhang et al. 2011), and EMO (Zhou et al. 2011). There is no survey that covers EML techniques for different tasks with a non-technical presentation to reach a broader range of readers. Given the rapid development and growth of this field and its role in facilitating more ML applications, this paper aims to provide comprehensive survey on using EC techniques for major ML tasks. The remainder of this section briefly summarises of the current EML applications in different domains.

### 1.1. Current Evolutionary Machine Learning Applications

EML methods have been widely applied to real-world problems in various fields, including agriculture, manufacturing, power and energy, internet/wifi/networking, financial, and healthcare.

In agriculture, EML techniques have been used to plan agricultural land use (Kaim et al. 2018). The decision making in farming, e.g., fishing (Cobo et al. 2018) and crop farming (Pal et al. 2016), have also been addressed by EML.

EML techniques have been widely applied to manufacturing in different industries such as milk/dairy production (Lutton et al. 2014; Notte et al. 2016), wine production (Mohais et al. 2012), wood production (Zhao et al. 2017), mineral processing (Yu et al. 2011), transportation scheduling for seafood and milk products (Sethanan and Pitakaso 2016). EML methods can find solutions that help to reduce time and cost for both production and transportation. Supply chain is another important field highly related to manufacturing but integrates more sectors. EML methods have been employed to optimise the supply chain of food (Cheraghalipour et al. 2018), fish (Tabrizi et al. 2018) and others (Zhang et al. 2017) to reduce inventory and cost.

EML techniques have been applied to the power and energy industry, e.g., predicting load forecasting in power system for efficient management (Liao and Tsao 2006) and allocating wind turbines (Hou et al. 2015).

Finance is another important application area of EML. Financial data is often time series data, which is very difficult for prediction or analysis due to the temporal nature of the data. EML methods have been widely employed to financial data analysis (Wagner et al. 2007), market price prediction (Bagheri et al. 2014), bankrupt ratio analysis (Lakshmi et al. 2016), and credit risk management (Srinivasan and Kamalakannan 2018).

In healthcare and biomedical applications, EML techniques have been developed for gene sequence analysis, gene mapping, structure prediction and analysis of DNA (Pal et al. 2006) and biomarker identification (Ahmed et al. 2014). Prediction of protein 3D structure has also been addressed by many EML methods (Correa et al. 2018; Gao et al. 2018). EML also shows promise in important applications such as drug discovery (Le and Winkler 2015) and materials design (Le and Winkler 2016) where the search space is effectively infinite.

In addition, EML techniques have been applied to predict natural disaster, especially earthquake (Asim et al. 2018; Scoble et al. 2013), and other real-world problems, such as web service composition (da Silva et al. 2016), cloud computing (Guzek et al.
cyber security (Buczak and Guven 2016), and video games (Yannakakis and Togelius 2018). Readers are referred to (Chiong et al. 2012) for more EML real-world applications.

1.2. Organisation

This paper is presented mainly in a task-based manner. The first three sections present EML algorithms for the classification, regression, and clustering. Sections 5 and 6 discuss two large EML application areas, computer vision, and scheduling and computational optimisation, respectively. Section 7 is dedicated to evolutionary deep learning, an emerging topic that gains more in ML. Emerging topics and current issues/challenges are described in Section 8. Finally, Section 9 concludes this paper. Due to the page limit, only some of the typical works are referred.

2. Evolutionary Computation for Classification

EML techniques have been widely used for classification. The aim of classification algorithms is to learn a model/classifier that can correctly classify unseen instances (test data) by observing a set of given instances (training data). Each instance is usually presented by a set of attributes/variables/features and a label. The quantity, quality, and representation of the data are important factors influencing the performance of the learned classifiers (Tran et al. 2016b).

Although classifier construction is the main task in classification, some other tasks related to data preprocessing are also important. The existence of irrelevant and redundant features negatively affects the performance of learning algorithms. Therefore, feature selection/dimensionality reduction is widely used to remove irrelevant and redundant features, which effectively reduces the search space of a problem and hence improves the learning ability and the running time. Feature construction is also used to create high-level features that can better represent the problem.

The following subsections discuss the main EML techniques that have been proposed for these tasks and other related tasks such as unbalanced data and missing data.

2.1. EC for Classifier Construction

Many EML techniques have been used for classification such as GAs, GP, and PSO. GAs were the earliest EC technique used to evolve classification rules. Many methods have been proposed for general classification problems (Vivekanandan et al. 2013) as well as for specific domains such as text classification (Khaleel et al. 2016) and medical diagnosis (Fidelis et al. 2000). Chernbunmoong et al. (2015) proposed a GA-based method for activity classification where data from multiple sensors are used to recognise the activity of a person.

Using a similar vector representation to GAs, PSO has also been proposed for rule induction (Zheng et al. 2014). PSO has been shown to be more flexible than GAs and other classification algorithms.

Unlike PSO and GAs where individuals are represented using vectors, GP has more flexible representations. Discriminant functions are a form of mathematical expression which classify an instance into a class based on different thresholds (Espejo et al. 2010). With a tree-based representation, GP is well suited to developing discriminant
functions (Nag and Pal 2016). GP also has a long history in evolving decision trees (Zhao 2007) which are more effective than those developed by the traditional ways. GP is also used in inducing classification rules (Luna et al. 2014) which are more representative and use fewer conditions. Rivero et al. (2010) developed a GP-based method to automatically evolve artificial neural networks. LCS is also strong at evolving rules, having been applied in boolean function/classifier learning for multiplexer and even-parity problems (Iqbal et al. 2014).

In addition to evolving classifiers, GP can also deal with problems related to classification. Bhowan et al. (2014) proposed a GP-based classification method that can effectively cope with unbalanced data: a common problem where the number of instances in one class is much smaller than other class(es), e.g., malignant traffic is infrequent compared to normal traffic in network intrusion detection. Missing data is another common problem in real-world applications, which negatively affects the learning performance or makes some classification algorithms unusable. Considering predicting missing values as a regression task, Tran et al. (2018b) developed a GP-based imputation method that can effectively impute/predict missing values based on the other features.

Instance selection is used to reduce learning time by selecting a good subset of instances that allow maximum performance. EC techniques have been used for this task (Derrac et al. 2010).

By using a population-based search, EML techniques can evolve better classifiers than using greedy search methods, which use an heuristic for making locally optimal choices. Readers are referred to (Espejo et al. 2010) for further information.

2.2. EC for Feature Selection

Feature selection (FS) is a complex problem. With \( N \) original features, there are \( 2^N \) different feature subsets, which is impractical for exhaustive search on high-dimensional datasets (with thousands or more features). FS is challenging due to the large search space and possible interactions between features, which makes traditional greedy search prone to local optima. Many non-EC FS methods have been proposed, however these tend to be limited by these issues. With a population-based search, EC techniques have shown to be effective thanks to its global search and the ability of evolving and evaluating the whole feature subset considering possible interactions between features.

GAs are probably the first widely-applied EC technique to FS. GAs typically use an \( N \)-dimension binary vector to represent a feature subset where ‘1’ means the corresponding feature is selected and ‘0’ for not (Zhu et al. 2010). Many strategies have been proposed to improve GAs’ performance such as improving the crossover and mutation operators (Jeong et al. 2015), enhancing the initial population (Oreski and Oreski 2014) and using different feature subset evaluation methods (Xia et al. 2014; Xue et al. 2012) to better guide the search during the evolutionary process.

Although PSO was proposed much later than GAs, a larger number of PSO-based FS methods have been developed during the last decade (Xue et al. 2016). To represent a feature subset, PSO can use bit-strings (binary PSO) as GAs or continuous vectors (continuous PSO) where a threshold is used to determine if the corresponding feature is selected. Although binary PSO representation matches FS very well, its potential limitations lead to inferior performance compared to continuous PSO (Engelbrecht 2007). Unlike GA, PSO adjusts current individuals based on the communication between individuals about their best solutions found so far. Therefore, fruitful areas in
the search space can be quickly detected and used to guide the search. Researchers continue to improve PSO’s performance for FS in a number of ways including: initialisation strategies (Xue et al. 2014), representation (Tran et al. 2018a), updating mechanisms (Gu et al. 2018), integrating local search (Tran et al. 2016a), and evaluating features based on its intrinsic characteristics (aka filter approach) (Nguyen et al. 2016) and performance of learning algorithms (aka wrapper approach) (Xue et al. 2014).

Thanks to the implicit FS process in building GP trees, GP has been proposed for FS implicitly or explicitly. Implicit FS happens in all GP-based classification algorithms (Luna et al. 2014; Nag and Pal 2016). Explicit FS methods using GP have also been proposed for feature subset selection (Sandin et al. 2012), feature subset ranking (Neshatian and Zhang 2009a), and feature space exploration (Neshatian and Zhang 2009b). More information about FS using EC can be found in (Xue et al. 2016).

2.3. EC for Feature Construction

Besides FS, feature construction (FC) is another technique to enhance the representation of the feature space. FC combines the original features to construct new high-level features with better discriminating ability. The created features can be used to augment the original ones (Muharram and Smith 2005) or replace them as a dimensionality reduction solution (Neshatian et al. 2012; Tran et al. 2017).

Compared with FS, FC is more challenging due to its larger search space as it needs to choose not only a good subset of features but also an appropriate set of operators to combine them. The optimal model (whether linear or non-linear) to combine the original features is unknown in practice. With a flexible representation and a global search mechanism, GP can automatically evolve models without assuming any model structure. Constructed features can be represented with tree-based GP, where leaf nodes are features/constants and internal nodes are operators.

Many GP-based FC methods have been proposed using single-tree (Neshatian et al. 2012) or multiple-tree representations (Krawiec 2002; Tran et al. 2017). GP is used to construct features that are generally good for all classes (class-independent) (Krawiec 2002) or for a specific class (class-dependent) (Neshatian et al. 2012; Tran et al. 2017). Different approaches are also used to evaluate the constructed features during the evolutionary process such as filter (Tran et al. 2017), wrapper (Smith and Bull 2005), or a combination of both (Tran et al. 2016b).

Although GP has shown to be one of the most suitable techniques for FC, other EC algorithms have also been proposed and shown promise for FC such as GAs (Alfred 2008) and PSO (Dai et al. 2014).

3. Evolutionary Computation for Regression

Regression is a major ML task that attempts to identify and express the underlying relationship between the input features/variables and the target variable(s). Regression analysis is utilised for forecasting in widespread areas, e.g. finance, traffic, medicine, and biology (Xiong et al. 2014; Glaeser and Nathanson 2017). To build a regression model, two essential aspects need to be distinguished, i.e. the mathematical form/structure of the model, and the values of coefficients in the model. Many EC techniques have been proposed for the two aspects.
3.1. **EC for Regression Tasks**

**Model identification:** GAs have been used for model identification for linear regression, i.e. to identify and include only the input variables that are really important for explaining the target variable(s) (Sessions and Stevans 2006). Paterlini and Minerva (2010) developed a new GA method which not only selects the input variables but also determines the most appropriate mathematical transformations on these variables. A multi-objective GA method (Sinha et al. 2015) was proposed to identify regression models with a good balance between the empirical error and the model complexity. An evolutionary algorithm was proposed for fuzzy regression by choosing the best fuzzy function within a predefined library (Buckley and Feuring 2000). PSO was used to generate the structures of the fuzzy models in nonlinear polynomial form (Chan et al. 2011).

**Parameter estimation:** A large number of EC methods were proposed for parameter estimation for complicated or non-differentiable regression models. A GA method (Zhou and Wang 2005) was utilised to learn the minimum value of the least absolute deviation function for measuring the robustness of linear regression models. The effort of GA with seven different crossover operators on parameter estimation has been examined (Kapanoglu et al. 2007). The convergence of the GA method was explained by analysing the convergence of parameters in regression models with different levels of difficulty. GAs were extended to learn parameters in regression models for time series data (Kang et al. 2017). Chen et al. (2010) employed PSO to optimise the parameters for orthogonal forward regression.

3.2. **EC for Symbolic Regression**

Some EC techniques for regression are able to learn directly from the data and evolve both the structure and the parameters of the regression models simultaneously. This kind of regression tasks is known as **symbolic regression**. The distinguishing characteristic of symbolic regression is its interpretability, which can provide domain experts with meaningful insight into the underlying data generating process and highlight the most relevant features.

3.2.1. **GP for symbolic regression**

The symbolic nature of GP solutions and its flexible representation make GP a very suitable approach for symbolic regression. There are many successful applications of GP for symbolic regression (Vyas et al. 2018).

**Interpretability** is a distinct property of symbolic models, with which the models are able to distil novel knowledge (Schmidt and Lipson 2009). Many studies have been proposed to improve the interpretability of models evolved by GP. A typical approach is introducing *parsimony pressure* into GP, which considers the size of the solutions in their fitness evaluation. Parsimony pressure has been added to the fitness function as a linear term (Zhang and Mühlenbein 1995) or as an adaptive penalty regarding the growth metrics in the individuals and the population (Poli and McPhee 2008). GP equipped with instance sampling was shown to produce compact models with better prediction performance (Gonçalves and Silva 2013). A new feature selection method based on a permuting test was developed for GP for symbolic regression and regression models were shown with good interpretability (Chen et al. 2017).

**Prediction/generalisation ability** is another important metric for regression
techniques. The validation set, which is the most widespread mechanism for improving generalisation in ML, was also used for symbolic regression (Schmidt and Lipson 2009). Interval arithmetic was proposed to ensure that the evolved models do not have an undefined behaviour on unseen data (Keijzer 2003). Geometric semantic GP (Moraglio et al. 2012), which drives the search in GP by the semantic information, has shown to have good prediction performance (Chen et al. 2018b).

Controlling the functional complexity of models is an effective method to improve prediction performance. Tikhonov regularisation was introduced into GP to control model complexity (Ni and Rockett 2015). Order of nonlinearity uses the minimum degree of Chebyshev polynomials to approximate the complexity of GP models (Vladislavleva et al. 2009). Chen et al. (2018) introduced Vapnik-Chervonenkis (VC) dimension to directly measure and control the complexity of GP solutions.

3.2.2. Other EC Techniques for Symbolic Regression

Some other EC techniques are also available for symbolic regression. However, most of them are in their initial stage. LCS has been used for symbolic regression for the first time (Naqvi and Browne 2016). AIS (Johnson 2003), which is inspired by the natural immune systems in responding to attacks on an organism, was applied to solve symbolic regression tasks. Grammatical evolution (O’Neill and Ryan 2001), which evolves binary strings to select production rules in a grammar definition to generate any kind of programs, can also be used for symbolic regression.

4. Evolutionary Computation for Clustering

Often, data may have no labels and so the previously discussed supervised ML methods cannot be used. ML algorithms developed for this scenario are called unsupervised learning algorithms, which discover underlying patterns within the data (Nanda and Panda 2014). There are several approaches to this problem but the most studied is clustering. Clustering algorithms split a dataset into a set of clusters, so that data within a cluster are similar, while data in distinct clusters are different. A good clustering result (partition) gives insight into a dataset by splitting it into “natural” groups. Clustering is widely used in real-world tasks such as text mining, bioinformatics, and image categorisation (Nanda and Panda 2014).

EML has been widely applied to clustering problems (Hruschka et al. 2009) due to its ability to find good partitions in reasonable computational time on “big data” or when the number of clusters (K) is not known in advance (García and Gómez-Flores 2016). The field of EC clustering algorithms can be split into two categories: fixed algorithms that require that K is known, and automatic algorithms which discover K themselves. Fixed clustering algorithms are prevalent historically, whereas most recent work tackles the more difficult automatic clustering problem. The third category of algorithms which has emerged recently uses feature reduction to improve clustering performance. Traditional clustering approaches assume all features of a dataset to be equally useful. This is often untrue: for example, clustering weather records by “day of week” is clearly less useful than by “daily rainfall”. This becomes even more problematic in high-dimensional datasets. EC has recently been used to reduce the dimensionality of data in clustering (Alelyani et al. 2013). Each of these three categories will be discussed in turn.
4.1. Evolutionary Fixed Clustering

The first EC methods used for clustering were GAs, and this continues to be the most popular approach. Initial work (Krovi 1992) used primitive encodings (representations) on small datasets, with two or three clusters and at most 150 instances. Since then, substantial progress has been made on extending GAs to much more difficult problems, with over 40 clusters, and thousands of instances. Several new encoding schemes have been proposed that are suited to different clustering problems (Hruschka et al. 2009).

The label-based encoding scheme represents a partition as a vector of length \( N \) for \( N \) instances, where each instance has a label of the cluster it is in. This encoding was first proposed in the binary form \( (K = 2) \) (Krovi 1992), but more general forms have been explored since, such as bioinformatics with 16 clusters (Lu et al. 2004). In recent years, as clustering has been applied to larger datasets, this encoding is seldom used due to its inefficient representation.

The centroid-based encoding scheme is the most popular in recent EC clustering work, with an encoding length of \( K \times D \) for \( D \) dimensions in the data. This encoding represents each cluster by a set of \( D \) features which form the cluster centre (centroid). Each instance is assigned to the cluster whose centroid is closest by distance. One of the pioneering works in this field proposed a hybrid approach of a GA and \( k \)-means clustering to balance global and local search (Bandyopadhyay and Maulik 2002). PSO is also often used with this encoding as it can efficiently optimise real-valued problems. The first approach was proposed for image clustering (Omran et al. 2005), with good results compared to GA and traditional methods. Other swarm intelligence methods such as ACO have also seen some use (Handl and Meyer 2007).

GP has also been briefly investigated for fixed clustering. Multi-tree GP was proposed for clustering, where each tree represents a cluster, and an instance is assigned to the tree producing the maximum output (Boric and Estévez 2007). GP is also used to build ensembles of clustering algorithms to produce more robust and accurate partitions (Coelho et al. 2011).

4.2. Evolutionary Automatic Clustering

One of the seminal works in evolutionary automatic clustering is MOCK (Handl and Knowles 2007). MOCK uses a graph-inspired label (locus) GA representation, where each instance’s label indicates an instance it has an edge to. The set of graphs in this encoding represents the set of clusters. This encoding is shape-invariant, i.e. clusters are not assumed to be a certain shape (e.g. hyper-spherical) as in many clustering methods. The use of a multi-objective fitness function was also very novel. Recently, many EMO clustering methods have been proposed (García and Gómez-Flores 2016), including a number of extensions to MOCK (Garza-Fabre et al. 2018). Other graph-inspired techniques have been proposed, including GPGC, which uses GP to evolve tailored similarity measures for clustering problems (Lensen et al. 2017a).

A flexible-length centroid encoding (Sheng et al. 2016) and a medoid-based encoding have also been used for automatic clustering, primarily with GAs or PSO. A medoid-based encoding is a binary encoding of length \( N \), where an instance is coded as a “1” if it is a medoid and “0” if it is not. A medoid indicates that an instance is the centre of a cluster. This has the advantages of a fixed-length encoding, while also allowing \( K \) to be discovered automatically (Lensen et al. 2016).

Many other EC algorithms such as DE, ABC, and GP have also seen some use for automatic clustering (García and Gómez-Flores 2016).
4.3. Evolutionary Clustering with Feature Reduction

NMA_CFS (Sheng et al. 2008) was a pioneering GA method that simultaneously performs feature selection and clustering, selecting features tailored to the clusters found. Recently, PSO-based approaches have been investigated using sophisticated initialisation and local search methods (Lensen et al. 2017c). Feature weighting for clustering has also been proposed (O’Neill et al. 2018).

FC methods are very effective at improving performance in classification tasks (Espejo et al. 2010), but have seen little use in clustering. An initial wrapper approach was proposed using GP for FC to improve k-means clustering (Lensen et al. 2017b), and embedded approaches have also been proposed (Nanda and Panda 2014). Given the upsurge of high-dimensional data, it is expected that future evolutionary clustering work will focus on new ways of incorporating feature manipulation techniques into clustering.

5. Evolutionary Computer Vision

Utilising EML to tackle a variety of problems in different computer vision tasks have received more attention over the last few decades, e.g., image classification, image segmentation, object detection, feature extraction, image compression, image registration, image restoration, and image enhancement. Generally, EML for computer vision problems and applications can be categorised based on the application domain (e.g. medical, military, and environment), task (e.g. classification, segmentation, and feature manipulation), and the solution representation (e.g. tree structure, and chromosomes or strings of bits). A brief review of EML methods in computer vision is provided in the following subsections, and interested readers can check (Olague 2016).

5.1. EC Techniques for Image Preprocessing

Designing a method to handle tasks such as noise cancellation, image segmentation and image enhancement, often, requires human intervention and sufficient domain knowledge. EC techniques have been successfully utilised to automatically handle such tasks and such methods did not only remove/reduce the human intervention requirement, but also have been shown to evolve potentially better models compared to the hand-crafted domain-expert designed ones.

Image segmentation aims at dividing an image into different regions based on some criteria such as the connectivity of the pixels. GP has been applied to image segmentation by automatically evolving a similarity measure in (Vojodi et al. 2013). In (Liang et al. 2015), GP was used to segment objects of interest, whereas PSO was utilised for road signs segmentation (Mussi et al. 2010), and region of interest identification via image segmentation (Dhanalakshmi et al. 2016). Defining the threshold values for image segmentation is a challenging task that has been tackled using AIS (Cuevas et al. 2012). Other EC techniques, such as DE (Maulik and Saha 2009) and ACO (Tao et al. 2007), have been very promising to improve fuzzy clustering for image segmentation by grouping pixels into different clusters.

Detecting edges also represents a very important task that aims at finding the edges between different regions in an image, which helps in finding the boundaries of an object of interest. In (Lu and Chen 2008), ACO has been utilised to improve the performance of edge detection, whereas GP has been used to automatically evolve an
edge detector in (Fu et al. 2015).

Salient object detection (SOD) aims at identifying the most attention grabbing regions in an image, which represents a preprocessing task to focus the search into a specific part of the image. Finding an optimal set of weights for different features to improve SOD has been achieved by utilising PSO (Afzali et al. 2017).

5.2. EC Techniques for Image Feature Manipulation

Traditionally, building or training an image classifier requires a set of features as operating directly on raw pixel values is very challenging due to the large search space. Feature manipulation, including feature extraction, feature construction and feature selection, is very important in computer vision and pattern recognition.

GP has been utilised for automatically evolving models that improve existing image descriptors such as scale-invariant features (SIFT) (Hindmarsh et al. 2012), and speeded-up robust features (Perez and Olague 2013); whereas EMO is adopted for extracting image features (Albukhanajer et al. 2015).

Image descriptors aim at identifying different image keypoints, e.g., lines, corners and spots, in an image and generating the corresponding feature vector. In (Al-Sahaf et al. 2017), GP has been utilised to automatically evolve image descriptors that automatically detect designed keypoints for multi-class texture image classification. This method mimics the well-known and largely utilised local binary pattern (LBP) image descriptor. While both methods operate in a similar fashion, i.e., using a sliding window, they differ in being manually designed by domain-experts (LBP) or automatically designed by the evolutionary process. Moreover, LBP has been designed to detect a specific set of keypoints whereas GP-based descriptors automatically design the keypoints to be detected.

PSO has also been used in conjunction with SIFT for face recognition (Lanzarini et al. 2010). Furthermore, selecting optimal image features by utilising accelerated binary PSO is investigated in (Aneesh et al. 2011). In (Valarmathy and Vanitha 2017), AIS has been investigated to optimise image feature selection in MRI images.

5.3. EC Techniques for Object Detection and Image Classification

Object detection aims at localising the different objects in an image. In (Bhanu and Lin 2004), GP has been utilised and shown promise in this task.

Image classification is the task of categorising images into different groups or classes based on their visual content. In order to detect breast cancer in images, GP has been used to classify different cut-outs of medical images into malignant and benign classes (Ryan et al. 2015), whereas Ain et al. (2017) tackled the problem of skin cancer classification in images by utilising GP with a mix of biomedical and LBP features. A GP-based classification method for identifying active tuberculosis in X-ray images was proposed in (Burks and Punch 2018). Motivated by the promising results achieved in (Li and Ciesielski 2004), Abdulhamid et al. (2011) have further investigated the potential of utilising loops with GP for binary image classification and similar observations have been revealed based on the experimental results compared to that was found in (Li and Ciesielski 2004).

Feature extraction represents a very crucial task that aims at identifying and generating some informative features to discriminate the different classes/objects. GP has been shown to perform very well in this regard in (Al-Sahaf et al. 2012) and even with
the presence of noise in (Albukhanajer et al. 2015). Perez et al. (2010) utilised PSO to extract features for face and iris localisation, whereas PSO was employed for object recognition in (Perlin et al. 2008) and face recognition in (Ramadan and Abdel-Kader 2009).

Template matching is a well-known approach for object detection and recognition. An ACO-based method for fingerprint matching was proposed in (Cao et al. 2012), and the results have been shown to outperform the state-of-the-art methods.

Nevertheless, other EC techniques such as LCSs (Kukenys et al. 2011), and AISs (Wang et al. 2008) have been proposed for image classification, where an AIS based identity recognition system is proposed in (Silva et al. 2015).

6. Evolutionary Computation for Scheduling and Combinatorial Optimisation

Scheduling and combinatorial optimisation is an important research area with many real-world applications such as manufacturing and cloud computing. They have been studied extensively as pure optimisation problems. Recently, more research treat them as machine learning tasks due to the following two main motivations.

First, the environment is often dynamic in reality. For example, in manufacturing, job orders arrive in real time and need to be scheduled immediately. Traditional optimisation approaches such as mathematical programming and GAs are not fast enough to respond, and it is necessary to find a heuristic/rule that can generate/adjust the solution in real time effectively.

Second, manually designing an effective optimisation algorithm for a complex problem requires much domain expertise and time. Using ML techniques to automatically design algorithms/heuristics can save much human effort.

The ML approaches that search for promising heuristics are called hyper-heuristics (Burke et al. 2013). EC has been successfully applied as hyper-heuristics. In contrast to being used for conventional optimisation, the fitness evaluation is the key difference when EC is used as hyper-heuristics, where each individual is a heuristic. To evaluate a heuristic, it is applied to a set of training instances and generates solutions to them. The fitness of a heuristic is set as the average quality of the solutions it generates.

In the rest of this section, we will provide a brief review on evolutionary hyper-heuristics for classic problems including scheduling, routing and bin packing.

6.1. Evolutionary Hyper-heuristics for Scheduling

Scheduling (Pinedo 2016) aims to design a schedule to process a set of jobs by a set of machines with minimum cost/time. Dispatching rule is commonly used to generate schedules in an online fashion. GP-based Hyper-Heuristic (GPHH) has achieved great success in automatically designing dispatching rules.

In a standard job shop scheduling problem, a dispatching rule is invoked whenever a machine becomes idle. It uses a priority function to prioritise the jobs in the machine’s queue, and decides the job to be processed next. There have been a number of studies on developing GPHH to evolve such priority functions for the standard job shop scheduling problem (Mei et al. 2016, 2017).

In addition to the standard job shop scheduling problem, people have also applied GPHH for solving other problem variants, such as multi-objective job shop scheduling (Nguyen et al. 2014) and flexible job shop scheduling (Yska et al. 2018). Branke et al.
(2016) and Nguyen et al. (2017) give comprehensive surveys of this area.

**6.2. Evolutionary Hyper-heuristics for Routing**

A routing problem seeks optimal routes subject to some constraints, e.g. serving all the customers for delivery or visiting all the attractions in a trip.

(Oltean and Dumitrescu 2004) employed GPHH to evolve heuristics for travelling salesman problem, which decides the next node to be added into the current partial tour. (Weise et al. 2012) developed a GPHH algorithm to evolve heuristics for the arc routing problem, which uses a vehicle to serve the streets on a road network, where each street has an uncertain request. Whenever the vehicle becomes idle, it calculates the priority of the remaining streets to decide the street to be served next. Here, GPHH evolves the priority function. (Liu et al. 2017) considered a more realistic problem model, and improved the performance of GPHH by designing more features. (Jacobsen-Grocott et al. 2017) developed a GPHH approach to vehicle routing problem with time windows, which serves the nodes rather than edges.

**6.3. Evolutionary Hyper-heuristics for Bin Packing**

Bin packing aims to minimise the number of bins to place all the items. A typical heuristic for bin packing starts with empty bins. Then, for each item, the heuristic calculates a priority value for each bin based on the current situation, and places the item into the bin with the best priority. Then, GPHH is employed to evolve the priority function. (Burke et al. 2006) developed GPHH for one-dimensional bin packing. (Burke et al. 2010) and (Allen et al. 2009) extended the problem to two-dimensional and 3-dimensional packing, respectively.

**7. Evolutionary Deep Learning**

Deep Learning (DL) has shown the remarkable performance in addressing increasingly complex data with large feature sizes from different domains such as images, gene expression, text and web mining (LeCun et al. 2015), owing to it automatic feature generation and selection capabilities (Bengio et al. 2009). Evolutionary DL (EDL) aims at using EC approaches to promoting the usability or improving the performance of DL algorithms. Existing EDL algorithms are mainly composed of neural network-based EDL (NN-EDL) algorithms and genetic programming-based EDL (GP-EDL) algorithms.

**7.1. Neural Network-based Evolutionary Deep Learning**

NN-EDL algorithms mainly focus on designing network architectures, optimising the weights, and solving multi-objective optimisation problems.

Existing approaches for designing architectures can be divided into two different categories: supervised NN-EDL and unsupervised NN-EDL. One typical work on NN-EDL for unsupervised deep learning is the EUDNN method (Sun et al. 2018). Existing supervised NN-EDL algorithms includes Large-scale Evolution (Real et al. 2017), EvoCNN (Sun et al. 2017), and so on.
There are two different strategies for searching for the best weights. The first is to directly encode the weights (Lehman et al. 2018). The second is to search for the best weights in an indirect way (Sun et al. 2018).

An NN-based deep learning algorithm with promising performance usually has a large number of parameters, which would take a large amount of computational resource. However, the computational resource is often limited, such as on mobile devices. In this regard, maximising performance and minimising computational resource are two conflicting objectives, i.e., a multi-objective (MO) optimisation problem. NN-EDL for MO has been first pointed out by Sun et al. (2017), and then is specifically investigated by Dong et al. (2018).

Because NN-based DL often has large number of parameters, some high-performance hardware has been developed to accelerate their performing, such as graphic processing unit (GPU), field-programmable gate array (FPGA) and tensor processing unit (TPU).

### 7.2. GP-based Evolutionary Deep Learning

GP has been developed to achieve DL without NNs. The flexible structure of GP allows it to learn abstract and compact representation with suitable model complexity in a layer-by-layer feature transformation manner, which meet the key points of DL.

GP-EDL has been developed to integrate multiple steps to learn a single high-level feature for image classification in a single GP tree. The first method is perhaps the multi-tier GP with an image filtering tier, an aggregation tier and a classification tier to perform region detection, feature extraction, feature construction, and image classification, simultaneously (Atkins et al. 2011). Bi et al. (2018) proposed a multi-layer GP method with a utilisation of image-related operators to learn high-level features for image classification.

GP-EDL has been proposed to learn multiple features instead of a single feature from raw data. Shao et al. (2014) proposed a multi-objective GP with a multi-layer structure to learn features for difficult image classification tasks. Agapitos et al. (2015) developed a greedy layer-wise deep GP method with a filter bank layer, a transform layer, an average pooling layer, and a classification layer for object recognition. Later, Rodriguez-Coayahuitl et al. (2018) defined the structured layered GP for representation learning and introduced deep GP.

### 8. Emerging Topics and Current Issues

This section provides a number of emerging topics and summarises the major issues/challenges in EML.

#### 8.1. Emerging Topics

**Evolutionary Transfer Learning:** Transfer learning becomes increasingly popular in ML in recent years. It aims to improve the performance of learning algorithms in the target tasks/domains by using useful knowledge extracted from the source tasks/domains (Pan et al. 2010). In transfer learning, there are three research issues: what to transfer, when to transfer and how to transfer (Pan et al. 2010).

Recently, transfer learning methods have been developed to enhance EC methods.
The transferred knowledge includes subtree of GP (Iqbal et al. 2017), parameters of DE (Gong et al. 2015), and the probability distributions of solution (Jiang et al. 2018). However, the four main transfer learning methods, instances transfer, feature representation transfer, parameter transfer, and rational-knowledge transfer (Pan et al. 2010), have not been extensively investigated in EC. Moreover, instead of using transfer learning in EC, the applications of EC to transfer learning are expected to be addressed in the future.

**Evolutionary Ensemble Learning:** Ensemble learning is an important area in ML. Ensemble learning algorithms learn multiple learners/models from the training data to solve a problem. An ensemble consists of a number of base learners, which are learnt using traditional learning algorithms. Commonly used ensemble methods include bagging, boosting and stacking (Zhou 2012). Generally, to construct a strong ensemble, the base learner needs to be accurate and diverse (Zhou 2012).

EC methods have been combined with learning algorithms to obtain a strong ensemble. For example, de Araújo Padilha et al. (2016) developed a multi-level approach using GA to learn ensembles of SVM and Pulido et al. (2014) applied PSO to optimise ensembles of NNs. EC methods have been developed to evolve ensembles using ensemble methods such as bagging and boosting (Folino et al. 2006). EMO algorithm is effective for obtaining a set of solutions with high diversity, which has been cooperated with ensemble methods on difficult problems (Bhowan et al. 2013). However, there is still a large space on this promising topic, where EC methods can be further developed to address the diversity of base learners and the interpretability of the ensembles.

**Automated Machine Learning (AutoML):** AutoML is an emerging area in ML, which aims at automating ML techniques to allow people without ML domain knowledge to use them for problem solving. An AutoML method often integrates the data preprocessing, feature engineering, and learning processes, where the selection and the hyper-parameters of these methods are optimised by an optimisation technique. Well-known AutoML methods include Auto-WEKA, Auto-Sklearn and Auto-Keras, which are based on existing ML libraries.

EC methods have also been employed in AutoML. For example, the well-known tree-based pipeline optimization tool (TPOT) uses GP to evolve a set of data transformations and ML models (Olson and Moore 2016). Chen et al. (2018a) developed an Autostacker method, where an EC algorithm was used to find the optimal hyper-parameters for ML pipelines. Besides the achievements of these methods, there are still many unexplored opportunities in this topic, such as EMO for AutoML, which needs to be investigated in the future.

### 8.2. Current Issues

Despite its successes, EML remains a promising field with challenges and opportunities. This section discusses some of its major issues in theoretical foundation, computational cost, scalability, generalisation, and interpretability.

There is some theoretical analysis of EML methods on running time, convergence guarantee and parameter settings (Auger and Doerr 2011). However, current EML methods still lack of mathematics proof such as on results, which might prevent scientists and practitioners from using EML methods.

Being computationally expensive is a major issue of the existing EML methods. EML methods are population-based and need to evaluate a population of individuals/solutions at each generation, which often makes the methods more expensive than
many traditional ML methods.

Scalability is a common problem in EML, where the learning methods cannot scale well when the datasets become bigger. An increase in the number of features and the number of instances often requires larger memory and longer computation time. This might limit the applications of EML methods to large-scale problems.

Like most ML techniques, EML methods also face the challenge of poor generalisation, which may due to insufficient data, overfitting, poor feature choice or availability. For EML methods, poor generalisation often refers to the problem of overfitting, which means that the learned model can perfectly fit to the training data, but sometimes work poorly on the unseen data. The issue of overfitting in EML needs further investigation in the future.

Interpretability is another important issue in EML and ML. Good interpretability of the learnt models not only provides more insights in why they are better/worse, but also improves the acceptance and reuse. Among EML methods, several methods such as GP use a tree-based representation having good interpretability of solutions, which can be further investigated in the future.

Except for the aforementioned issues, many other problems in EML can be further addressed, such as EML on missing data, noisy data and unbalanced data.

9. Conclusions

This paper provided a concise review of major EC techniques for ML tasks, which covers both supervised and unsupervised tasks and applications. In addition to a number of emergent techniques such as evolutionary deep learning and transfer learning, this paper also discussed major current issues and challenges in this area, including scalability, generalisation, and interpretability/compressibility of the evolved models.

Having said that, the fast development of the hardware such as GPU devices and cloud computing facilities has been making previously impossible EML tasks become reality. The involvement and investment from large IT companies such as Google, Microsoft, Uber, Huawei and IBM have been making EML methods more practical. It is expected that EML methods will play a significant role in AI and ML in the next ten years. EML is expected to be applied to most real-world data mining and big data tasks and applications in our daily life. In the future, the AI and EC/ML group at Victoria University of Wellington will seek research collaborations with colleagues who are interested in AI in science, engineering, commerce/business, humanities and social sciences, education and law as well as the primary industry in New Zealand.

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